RUTGERS Edward J. Bloustein School of Planning and Public Policy

Role of Governance in Independent Decision Making for Building Electric Infrastructure Resilience

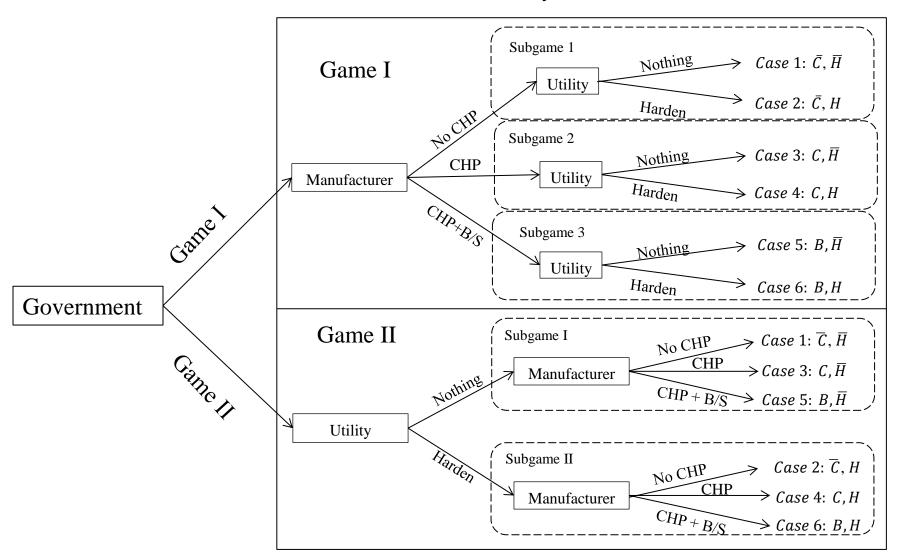
TAI Washington DC Nov 7, 2014

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Outline

- Introduction and background
- Sequential game-theoretic model of Government, Utility and Manufacturer
- 2 Key questions
 - Does order of decision-making between Utility and Manufacturer matter?
 - What might happen in reality?
- Conclusion

Game formulation when either manufacturer or utility moves first



Public vs. Private resiliency investments



Use alternate materials for stronger poles

http://www.fplenergyservices.com/storm/stormsecure/hardening.shtml



Flood walls

Photo: Brian A. Pounds

Source: http://www.ctpost.com/local/article/UI-hardens-substations-against-high-water-4682439.php



Combined Heat-Power Plant (CHP)

http://www.cospp.com/articles/print/volume-11/issue-2/Project_Profile/cogeneration-plant-to-boost-output-at-dubai-aluminium.html



Diesel backup generator

http://www.shutterstock.com/pic-88581673/stock-photo-high-voltage-industrial-standby-diesel-generator-at-a-power-generation-plant-in-a-textile-factory.html

Notation	Description
l = 24	Outage length (Hrs)
$p_H^l=0.1$	Probability of l -hour outage in a year given grid is hardened (%)
$p_N^l = 0.8$	Probability of l -hour outage in a year given grid is not hardened (%)
K = 1	Cost of grid hardening (\$million) to Utility
$c_H = 0.1$	Cost of grid hardening (\$million) to Manufacturer
$V^M(l) = 5,000$ $V^W(l) = 50,000$	Value of lost load (VOLL) from an l -hour outage for Manufacturer and the other customer (kWh)
$h_O = 8,322$	Hours of CHP operation in a year (Hrs) implying Capacity Factor=95%
$e^W(t) = 15.7^{\text{ a}}$	Cost of annual electricity consumption (\$million) for the other customer
i = 0.59	Incentive given to Manufacturer for installing a CHP (\$million) regardless of blackstart capability
$e^M(t) = 1.57^{\text{ a}}$	Cost of annual electricity consumption (\$million) to Manufacturer
$e_c^M(t) = 0.42^{\mathrm{a}}$	Cost of annual electricity consumption with a CHP (\$million) to Manufacturer

Notation	Description
M = 8,760	Hours in a year (Hrs)
t	Time period (y), from 0 to 20 years
k = 1,070	CHP electric capacity (kW)
c = 3.82	Cost of buying a CHP (\$million)
b = 3.958	Cost of buying a CHP with black-start capability (\$million)
$c_O(h_O) = 0.1^{\mathrm{a}}$	Annual operation and maintenance cost of a CHP (\$million)
D = 1,200, $D^W = 12,000$	Manufacturer's and the other customer's average hourly demands (kW)
$S(h_O, D) = 0.11^{\mathbf{a}}$	Annual standby charge (\$million)
g=0.62 a	Cost of annual gas consumption (\$million) to Manufacturer
$g_c = 1.09$ a	Cost of annual gas consumption with a CHP (\$million) to Manufacturer
$r^e = 1.98$	Electric tariff escalation (% per year)
$r^g = 3.20$	Gas tariff escalation (% per year)
d = 8	Discount rate (% per year)

Manufacturer: CHP+B/S, Utility: Harden

Manufacturer payoff:

$$\underbrace{\left(\frac{\sum_{l}p_{N}^{l}*(M-l)+(1-\sum_{l}p_{N}^{l})*M}{M}\right)}_{} *\underbrace{\left(e^{M}+g\right)} + \underbrace{\sum_{i}p_{N}^{i}}_{} *\underbrace{\underbrace{l\cdot p\cdot v^{N}(l)}+\underbrace{b-i+c_{N}}_{}}_{}$$

(Prob. of Normal Operation) (Energy Use without CHP) (Prob. of Outage) (VOLL) (Capital Costs)

$$+\sum_{t=1}^{20} \left(\frac{\sum_{l} v_{N}^{l} * (N-l) + \left(1 - \sum_{l} v_{N}^{l}\right) * N}{N} \right) * \left(\frac{e^{N} + g_{e} + S(h_{o}, D) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{1 - d}{1 + \sum_{t=1}^{20} \sum_{l} p_{N}^{l}} * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{1 - d}{1 + \sum_{t=1}^{20} \sum_{l} p_{N}^{l}} * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{1 - d}{1 + \sum_{t=1}^{20} \sum_{l} p_{N}^{l}} * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{1 - d}{1 + \sum_{t=1}^{20} \sum_{l} p_{N}^{l}} * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{1 - d}{1 + \sum_{t=1}^{20} \sum_{l} p_{N}^{l}} * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{1 - d}{1 + \sum_{t=1}^{20} \sum_{l} p_{N}^{l}} * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{1 - d}{1 + \sum_{t=1}^{20} \sum_{l} p_{N}^{l}} * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{1 - d}{1 + \sum_{t=1}^{20} \sum_{l} p_{N}^{l}} * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) * \left(\frac{g^{b}(l) + c_{o}(h_{o})}{(Energy \& OM Costs with CHP)} \right) *$$

Utility payoff:

$$\underbrace{ \begin{array}{c} \text{Year 0} \\ \text{$K-\sum_{l} f_{K}(1-d)^{s}$} \end{array} - \underbrace{ \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + (1-\sum_{l} p_{N}^{l}) * M}{M} \right) }_{\text{M}} * \underbrace{ \left(e^{M} + e^{W} \right) }_{\text{M}} + \underbrace{ \begin{array}{c} \sum_{l} p_{N}^{l} * (M-l) + (1-\sum_{l} p_{N}^{l}) * M \\ M \end{array} \right) }_{\text{M}} * \underbrace{ \left(e^{M} + e^{W} \right) }_{\text{M}} * \underbrace{ \left(e^{M} + e^{W} \right) }_{\text{M}} + \underbrace{ \begin{array}{c} \sum_{l} p_{N}^{l} * (M-l) + (1-\sum_{l} p_{N}^{l}) * M \\ M \end{array} \right) }_{\text{M}} * \underbrace{ \left(e^{M} + e^{W} \right) }_$$

(Capital Costs with Overtime Return)(Prob. of Normal Operation)(Electricity Tariff)

(Prob. of Outage)

(Electricity Tariff) (Discount)

Society payoff:

$$\underbrace{\left(\frac{\sum_{l} p_{N}^{l} * (M-l) + (1-\sum_{l} p_{N}^{l}) * M}{M}\right)}_{\mathbf{M}} * (e^{M} + \mathbf{g}) + \sum_{l} \underbrace{p_{N}^{l}}_{\mathbf{N}} * \underbrace{1 \cdot p \cdot \left(p^{N}(l) + p^{N}(l)\right)}_{\mathbf{M}} + \underbrace{b + c_{N}}_{\mathbf{N}}$$

(Prob. of Normal Operation) (Energy Use without CHP) (Prob. of Outage) (VOLL) (Capital Costs)

Year 1-20

$$+\sum_{t=1}^{20} \left(\frac{\sum_{l} v_{N}^{l} * (M-l) + \left(1 - \sum_{l} v_{N}^{l}\right) * M}{M} \right) * \underbrace{\left(g_{c} + S(h_{o}, D) + c_{o}(h_{o}) - u * n(h_{o})\right)}_{M} * \underbrace{\left(1 - d\right)^{t} + \sum_{t=1}^{20} \underbrace{\sum_{l} p_{N}^{l}}_{M} * \underbrace{\left(g_{c}^{b}(l) + c_{o}(h_{o}) + p * v^{w}(l)\right)}_{M} * \underbrace{\left(1 - d\right)^{t}}_{M} * \underbrace{\left(1 - d\right)^{t}}$$

(Prob. of Normal Operation) (Gas& OM Costs with CHP - Emission Reduction) (Discount) (Prob. of Outage)(Gas& OM Costs with CHP & VOLL at outage)(Discount)

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Optimizing Electric Distribution Reliability

Case	Manufacturer Payoff	Utility payoff	Society payoff
1. <i>Ē</i> , Ħ	$\sum_{t} \left(\frac{\sum_{l} p_{N}^{l} * (M - l) + (1 - \sum_{l} p_{N}^{l}) * M}{M} \right) * (e^{M} + g) * (1 - d)^{t} + \sum_{t} \sum_{l} p_{N}^{l} * l * D * V^{M}(l) * (1 - d)^{t} \right)$	$-\sum_{t} \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M} \right) \\ * (e^{M} + e^{W}) * (1 - d)^{t}$	$\sum_{t} \left(\frac{\sum_{l} p_{N}^{l} * (M - l) + (1 - \sum_{l} p_{N}^{l}) * M}{M} \right) $ $* (e^{M} + g) * (1 - d)^{t} $ $+ \sum_{t} \sum_{l} p_{N}^{l} * l * (D * V^{M}(l) + D^{W} * V^{W}(l)) * $ $- d)^{t}$
2. <i>Ĉ</i> , <i>H</i>	$c_{H} + \sum_{t=1} \left(\frac{\sum_{l} p_{H}^{l} * (M - l) + \left(1 - \sum_{l} p_{H}^{l}\right) * M}{M} \right) \\ * (e^{M} + g) * (1 - d)^{t} \\ + \sum_{l} \sum_{l} p_{H}^{l} * l * D * V^{M}(l) * (1 - d)^{t} \\ - d)^{t}$	$K - \sum_{t} fK(1-d)^{t}$ $- \sum_{t} \left(\frac{\sum_{l} p_{H}^{l} * (M-l) + (1 - \sum_{l} p_{H}^{l}) * M}{M} \right) * (e^{M} + e^{W}) * (1-d)^{t}$	$K - \sum_{t} fK(1-d)^{t} + c_{H}$ $+ \sum_{t} \left(\frac{\sum_{l} p_{H}^{l} * (M-l) + \left(1 - \sum_{l} p_{H}^{l}\right) * M}{M} \right)$ $* (e^{M} + g) * (1-d)^{t}$ $+ \sum_{t} \sum_{l} p_{H}^{l} * l * (D * V^{M}(l) + D^{W} * V^{W}(l)) *$ $- d)^{t}$
3 . <i>C</i> , <i>H</i>	$c - i + \left(\frac{\sum_{l} p_{N}^{l} * (M - l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M}\right)$ $* (e^{M} + g)$ $+ \sum_{t=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M - l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M}\right) * (e_{c}^{M})$ $+ g_{c} + S(h_{o}, D) + c_{o}(h_{o})) * (1 - d)^{t}$ $+ \sum_{t} \sum_{l} p_{N}^{l} * l * k * V^{M}(l) * (1 - d)^{t}$	$-\left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M}\right)$ $* (e^{M} + e^{W})$ $-\sum_{t=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M}\right)$ $* (e_{c}^{M} + e^{W}) * (1 - d)^{t}$	$c + \left(\frac{\sum_{l} p_{N}^{l} * (M - l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M}\right)$ $* (e^{M} + g) * (1 - d)^{t}$ $+ \sum_{l} \left(\frac{\sum_{l} p_{N}^{l} * (M - l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M}\right)$ $* (e_{c}^{M} + g_{c} + S(h_{o}, D) + c_{o}(h_{o}) - u * n(h_{o}))$ $* (1 - d)^{t}$ $+ \sum_{l} \sum_{l} p_{H}^{l} * l * (D * V^{M}(l) + D^{W} * V^{W}(l)) *$ $- d)^{t}$

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Optimizing Electric Distribution Reliability

Case	Manufacturer Payoff	Utility payoff	Society payoff
4. C , H	$\begin{split} c - i + c_H + & \left(\frac{\sum_l p_H^l * (M - l) + \left(1 - \sum_l p_H^l\right) * M}{M} \right) * \left(e^M + g \right) \\ + & \sum_{t=1}^{20} \left(\frac{\sum_l p_H^l * (M - l) + \left(1 - \sum_l p_H^l\right) * M}{M} \right) * \left(e_c^M + g_c \right) \\ + & S(h_o, D) + c_o(h_o) \right) * (1 - d)^t \\ + & \sum_t \sum_l p_H^l * l * k * V^M(l) * (1 - d)^t \end{split}$	$\begin{split} &K - \sum_{t} fK(1-d)^{t} \\ &- \left(\frac{\sum_{l} p_{H}^{l} * (M-l) + \left(1 - \sum_{l} p_{H}^{l}\right) * M}{M} \right) * \left(e^{M} + e^{W}\right) \\ &- \sum_{t=1}^{20} \left(\frac{\sum_{l} p_{H}^{l} * (M-l) + \left(1 - \sum_{l} p_{H}^{l}\right) * M}{M} \right) * \left(e_{c}^{M} \\ &+ e^{W}\right) * (1-d)^{t} \end{split}$	$\begin{split} c + c_{H} + K - & \sum_{t} fK(1 - d)^{t} \\ + & \left(\frac{\sum_{l} p_{H}^{l} * (M - l) + \left(1 - \sum_{l} p_{H}^{l} \right) * M}{M} \right) * (e^{M} + g) \\ + & \sum_{t=1}^{20} \left(\frac{\sum_{l} p_{H}^{l} * (M - l) + \left(1 - \sum_{l} p_{H}^{l} \right) * M}{M} \right) * \left(e_{c}^{M} + g_{c} \right) \\ + & S(h_{o}, D) + c_{o}(h_{o}) - u * n(h_{o}) \right) * (1 - d)^{t} \\ + & \sum_{t} \sum_{l} p_{H}^{l} * l * (D * V^{M}(l) + D^{W} * V^{W}(l)) * (1 - d)^{t} \end{split}$
5. B, \overline{H}	$\begin{split} b - \mathrm{i} + & \left(\frac{\sum_{l} p_{N}^{l} * (M - l) + \left(1 - \sum_{l} p_{N}^{l} \right) * M}{M} \right) * \left(e^{M} + \mathrm{g} \right) \\ + & \sum_{l} p_{N}^{l} * l * k * V^{M}(l) \\ + & \sum_{t=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M - l) + \left(1 - \sum_{l} p_{N}^{l} \right) * M}{M} \right) * \left(e_{c}^{M} + \mathrm{g}_{c} \right) \\ + & S(h_{o}, D) + c_{o}(h_{o}) * (1 - d)^{t} \\ + & \sum_{t=1}^{20} \sum_{l} p_{N}^{l} * \left(g_{c}^{b}(l) + c_{o}(h_{o}) \right) * (1 - d)^{t} \end{split}$	$\begin{split} &-\left(\frac{\sum_{l}p_{N}^{l}*\left(M-l\right)+\left(1-\sum_{l}p_{N}^{l}\right)*M}{M}\right)*\left(e^{M}+e^{W}\right)\\ &-\sum_{t=1}^{20}\left(\frac{\sum_{l}p_{N}^{l}*\left(M-l\right)+\left(1-\sum_{l}p_{N}^{l}\right)*M}{M}\right)*\left(e_{c}^{M}\\ &+e^{W}\right)*\left(1-d\right)^{t} \end{split}$	$\begin{split} b + & \left(\frac{\sum_{l} p_{N}^{l} * (M - l) + \left(1 - \sum_{l} p_{N}^{l} \right) * M}{M} \right) * (e^{M} + g) \\ + & \sum_{l} p_{N}^{l} * l * k * (V^{M}(l) + V^{W}(l)) \\ + & \sum_{l=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M - l) + \left(1 - \sum_{l} p_{N}^{l} \right) * M}{M} \right) * (e_{c}^{M} + g_{c} \\ + & S(h_{o}, D) + c_{o}(h_{o}) - u * n(h_{o}) \right) * (1 - d)^{t} \\ + & \sum_{t=1}^{20} \sum_{l} p_{N}^{l} * (g_{c}^{b}(l) + c_{o}(h_{o}) + l * D^{W} * V^{W}(l)) * (1 - d)^{t} \end{split}$
6. B, H	$\begin{split} b - \mathrm{i} + c_{\mathrm{H}} + & \left(\frac{\sum_{l} p_{\mathrm{H}}^{l} * (M - l) + \left(1 - \sum_{l} p_{\mathrm{H}}^{l} \right) * M}{M} \right) \\ * & \left(e^{M} + g \right) + \sum_{l} p_{\mathrm{H}}^{l} * l * k * V^{\mathrm{M}}(l) \\ + & \sum_{t=1}^{20} \left(\frac{\sum_{l} p_{\mathrm{H}}^{l} * (M - l) + \left(1 - \sum_{l} p_{\mathrm{H}}^{l} \right) * M}{M} \right) * \left(e_{\mathrm{c}}^{\mathrm{M}} + g_{\mathrm{c}} \right. \\ + & \left. S(h_{o}, D) + c_{o}(h_{o}) \right) * (1 - d)^{t} \\ + & \sum_{t=1}^{20} \sum_{l} p_{\mathrm{H}}^{l} * (g_{\mathrm{c}}^{\mathrm{b}}(l) + c_{o}(h_{o})) * (1 - d)^{t} \end{split}$	$\begin{split} &K - \sum_{t} fK(1-d)^{t} \\ &- \left(\frac{\sum_{l} p_{H}^{l} * (M-l) + \left(1 - \sum_{l} p_{H}^{l}\right) * M}{M} \right) * \left(e^{M} + e^{W}\right) \\ &- \sum_{t=1}^{20} \left(\frac{\sum_{l} p_{H}^{l} * (M-l) + \left(1 - \sum_{l} p_{H}^{l}\right) * M}{M} \right) * \left(e_{c}^{M} \\ &+ e^{W}\right) * (1-d)^{t} \end{split}$	$b + c_{H} + K - \sum_{t} fK(1 - d)^{t}$ $+ \left(\frac{\sum_{l} p_{H}^{l} * (M - l) + \left(1 - \sum_{l} p_{H}^{l}\right) * M}{M}\right) * (e^{M} + g)$ $+ \sum_{l} p_{H}^{l} * l * k * (V^{M}(l) + V^{W}(l))$ $+ \sum_{t=1}^{20} \left(\frac{\sum_{l} p_{H}^{l} * (M - l) + \left(1 - \sum_{l} p_{H}^{l}\right) * M}{M}\right) * (e_{c}^{M} + g_{c}$ $+ S(h_{o}, D) + c_{o}(h_{o}) - u * n(h_{o})) * (1 - d)^{t}$ $+ \sum_{t=1}^{20} \sum_{l} p_{H}^{l} * (g_{c}^{b}(l) + c_{o}(h_{o}) + l * D^{W} * V^{W}(l)) * (1$

Assumptions:

- 1. $e^M + g e_c^M g_c S(h_o, D) c_o(h_o) > 0$ (running CHP is cheaper than relying on the grid)
- 2. $l * D * V^M(l) (g_c^b(l) + S(h_o, D) + c_o(h_o)) > 0$ (during outage, running CHP with Blackstart is cheaper than the Value Of Lost Load)
- 3. $e^{M} > e_{c}^{M}$ (annual consumption of electricity is lower with CHP than that without CHP)
- 4. $p_N^l > p_H^l$ (probability of outage with a hardened grid would be lower than with an unhardened grid)
- 5. b > c (cost of CHP with Blackstart capability is higher than cost of CHP)

Key Question 1

DOES ORDER MATTER?

Under some conditions, order matters

- If costs of grid hardening, CHP & CHP+B/S are medium ($T_K^{34} < K < T_K^{12}$, $T_c^{23} < c < T_c^{24}$, $\max\{T_b^{46}, T_b^{25}\} < b < \min\{T_b^{15}, T_b^{35}\}$),
 - \bar{C} , H (Case 2) is optimal to Game I, where M moves first
 - B, \overline{H} (Case 5) is optimal to Game II, where U moves first
- How are thresholds defined?
 - T_K^{34} = U Payoff in Case 3 U Payoff in Case 4 +K (benefit of Harden for U given CHP)
 - T_c^{24} = M Payoff in Case 2 M Payoff in Case 4 c (benefit of CHP for M given Harden)
 - T_b^{46} = M Payoff in Case 4 M Payoff in Case 6 b (benefit of B/S for M given CHP & Harden)
- Both Manufacturer & Utility prefers Manufacturer to move first (\bar{C}, H) is better than B, \bar{H}

Society preference depends on benefit/cost of Harden and CHP with B/S

• Difference in society payoff $(C, H - B, \overline{H})$:

$$\underbrace{K - b} + \left(\frac{\sum_{l} p_{H}^{l} * (M - l) + \left(1 - \sum_{l} p_{H}^{l}\right) * M}{M}\right) * (e^{M} + g) - \left(\frac{\sum_{l} p_{N}^{l} * (M - l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M}\right) * (e^{M} + g)$$

Costs

Impact of Harden on normal energy consumption

$$+\sum_{t=1}^{\infty} \left(\frac{\sum_{l} p_{H}^{l} * (M-l) + \left(1 - \sum_{l} p_{H}^{l}\right) * M}{M} \right) * (e^{M} + g) * (1 - d)^{t} - \sum_{t=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M} \right) * \left(e_{C}^{M} + g_{C} + S(h_{o}, D) + c_{o}(h_{o}) - \mathbf{u} * \mathbf{n}(h_{o}) \right) * (1 - d)^{t} - \sum_{t=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M} \right) * \left(e_{C}^{M} + g_{C} + S(h_{o}, D) + c_{o}(h_{o}) - \mathbf{u} * \mathbf{n}(h_{o}) \right) * (1 - d)^{t} - \sum_{t=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M} \right) * \left(e_{C}^{M} + g_{C} + S(h_{o}, D) + c_{o}(h_{o}) - \mathbf{u} * \mathbf{n}(h_{o}) \right) * (1 - d)^{t} - \sum_{t=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M} \right) * \left(e_{C}^{M} + g_{C} + S(h_{o}, D) + c_{o}(h_{o}) - \mathbf{u} * \mathbf{n}(h_{o}) \right) * (1 - d)^{t} + \sum_{l=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M} \right) * (1 - d)^{t} + \sum_{l=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M} \right) * (1 - d)^{t} + \sum_{l=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M} \right) * (1 - d)^{t} + \sum_{l=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M} \right) * (1 - d)^{t} + \sum_{l=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M} \right) * (1 - d)^{t} + \sum_{l=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M} \right) * (1 - d)^{t} + \sum_{l=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M} \right) * (1 - d)^{t} + \sum_{l=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \left(1 - \sum_{l} p_{N}^{l}\right) * M}{M} \right) * (1 - d)^{t} + \sum_{l=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \sum_{l} p_{N}^{l}} * M}{M} \right) * (1 - d)^{t} + \sum_{l=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \sum_{l} p_{N}^{l}} * M}{M} \right) * (1 - d)^{t} + \sum_{l=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \sum_{l} p_{N}^{l}} * M}{M} \right) * (1 - d)^{t} + \sum_{l=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \sum_{l} p_{N}^{l}} * M}{M} \right) * (1 - d)^{t} + \sum_{l=1}^{20} \left(\frac{\sum_{l} p_{N}^{l} * (M-l) + \sum_{l} p_{N}^{l}} * M}{M} \right) * (1 - d)^{t} + \sum_{l} p_{N}^{l} * M}{M} \right) * (1 - d)^{t} + \sum_{l} p_{N}^$$

Benefit (impact) of & CHP+B/S (Harden) on normal energy consumption

$$+ \sum_{l} p_{H}^{l} * l * (D * V^{M}(l) + D^{W} * V^{W}(l)) - \sum_{l} p_{N}^{l} * l * (D * V^{M}(l) + D^{W} * V^{W}(l))$$

Benefit of Harden on VOLL

$$+\sum_{\underline{t}=1}\sum_{l}p_{H}^{l}*l*(D*V^{M}(l)+D^{W}*V^{W}(l))*(1-d)^{t}-\sum_{\underline{t}=1}^{20}\sum_{l}p_{N}^{l}*(g_{c}^{b}(l)+c_{o}(h_{o})+l*D^{W}*V^{W}(l))*(1-d)^{t}$$

Benefit of CHP+B/S (Harden) on VOLL

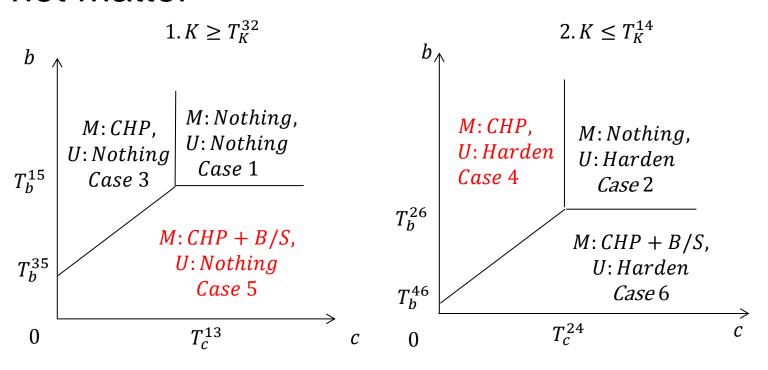
Requirements for existence

- $T_K^{34} < T_K^{12}$: benefit of Harden greater without CHP than with CHP due to assumptions 1 and 4 (cost is irrelevant) to Utility;
- $T_c^{23} < T_c^{24}$: benefit of Harden greater than cost given CHP $(T_c^{24} T_c^{23} = Case\ 2 Case\ 4 + c Case\ 2 + Case\ 3 c = Case\ 3 Case\ 4)$ to Manufacturer
- $T_b^{25} < T_b^{15}$: benefit of Harden greater than cost given no CHP $(T_c^{15} T_c^{25} = \text{Case } 1 \text{Case } 5 + b \text{Case } 2 + \text{Case } 5 b = \text{Case } 1 \text{Case } 2)$ to Manufacturer
- T_b^{25} < T_b^{35} : net benefit of CHP less than net benefit of Harden $(T_c^{35}-T_c^{25}=$ Case 3- Case 5+b- Case 2+ Case 5-b= Case 3- Case 2) to Manufacturer
- $T_b^{46} < T_b^{15}$: benefit of CHP+B/S greater than benefit of B/S given CHP & Harden
- $T_b^{46} < T_b^{35}$: benefit of B/S greater without than with Harden

What if existence conditions fail?

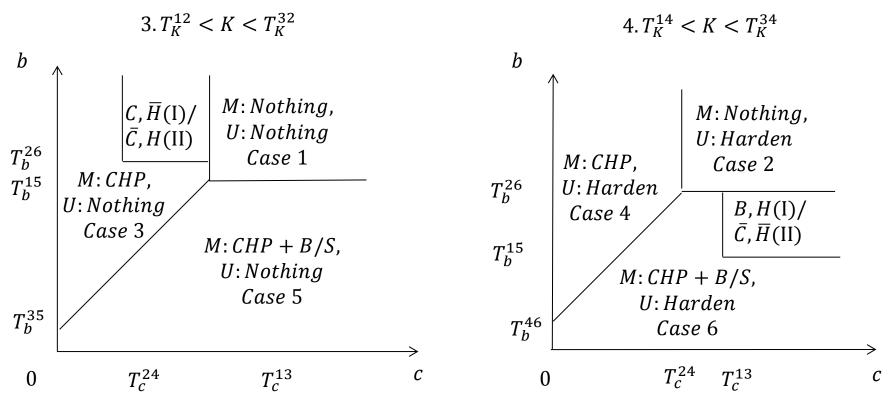
- $T_c^{23} > T_c^{24}$: benefit of Harden <u>less</u> than cost given CHP $(T_c^{24} - T_c^{23} = \text{Case } 2 - \text{Case } 4 + c - \text{Case } 2 + \text{Case } 3 - c = \text{Case } 3 - \text{Case } 4)$ to Manufacturer
- \bar{C} , H(Case 2) is optimal to both games
- Order does not matter
- Society can not induce B, \overline{H} (Case 5)

Large or small cost of Harden, then order does not matter



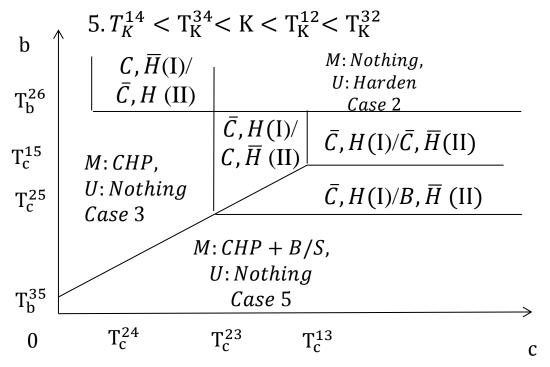
- Equilibriums are indicated (assuming M: CHP > Nothing regardless of Harden)
- Red could be socially desired outcomes
- Subsidizing CHP with/without Blackstart cannot prefer CHP to CHP+B/S

Relatively large or small K, order could matter



- If K relatively large, let M OR U move first depending on Society preferences over emission reduction & electricity reliability
- If K relatively small, let M move first to encourage B, H over \bar{C}, \bar{H}

Medium K, order more likely matters



- \bar{C} , \bar{H} is less likely to occur
- let M move first if both c & b are medium
- Let U move first if c is relatively small & b is large

Key question 2

WHAT IN REALITY?

RUTGERS

Optimizing Electric Distribution Reliability

Case	Manufacturer Payoff (\$million)	Utility Payoff (\$million)	Society Payoff (\$million)
1. \bar{c} , \bar{H}	27.44 = 26.11 (energy cost) + 1.33(VOLL)	-200.61 = -18.24(M)- 182.37(W)	37.72 = 26.11(energy cost) + 1.33(F VOLL) + 10.28(O VOLL)
2. ē, H	$26.39 = 26.16$ (energy cost) + 0.13 (VOLL) + $0.1(c_H)$	-199.99 = -18.27(M) - 182.72(W) + 1(K)	$28.82 = 26.16$ (energy cost) + 0.17(F VOLL) + 1.29(O VOLL) +1(K) + 0.1(c_H)
3. <i>c</i> , \overline{H}	25.47 = 18.97(energy cost) + 1.03(VOLL) + 3.82(CHP cost) – 0.59(CHP incentive)	-188.25 = -5.88(M)- 182.37(W)	32.97 = 18.97(energy cost) + 1.03(F VOLL) + 3.82(CHP cost) + 10.28(O VOLL) - 1.13(emission reduction)
4.c, H	$24.67 = 18.98$ (energy cost)+0.13(VOLL) + 3.82 (CHP cost) - 0.59 (CHP incentive) + $0.1(c_H)$	-187.61 = -5.89(M)- 182.72(W)+1(K)	$24.19 = 18.98$ (energy cost) + 0.13(F VOLL) + 3.82(CHP cost) + 1.29(O VOLL) +1(K) + 0.1(c_H) -1.13(emission reduction)
5. <i>b</i> , \overline{H}	22.34 = 18.97(energy cost) + 3.96(CHP cost) – 0.59(CHP incentive)	-188.25 = -5.88(M)- 182.37(W)	24.79 = 18.97(energy cost) +3.96(CHP cost) + 13.09(OVOLL)-1.13(emission reduction)
6. <i>b,H</i>	$24.69 = 18.98$ (energy cost) + 3.96 (CHP cost) - 0.59 (CHP incentive) + $0.1(c_H)$	-187.61 = -5.89(M)- 182.72(W) +1(K)	25.33= 18.98(energy cost) +3.96(CHP cost) + 1.29(O VOLL) +1(K) + 0.1(C_H)- 1.13(emission reduction) ₂₀

Equilibria

- Optimal: Manufacturer buys CHP+B/S & Utility Nothing regardless of order of moves
- Nothing is dominant strategy for Utility

$$- T_K^{14} = -200.61 + 188.61 + 1 = -11$$

$$- T_K^{34} = -188.25 + 187.61 + 1 = 0.36$$

$$- T_K^{12} = -200.61 + 199.99 + 1 = 0.38 \text{ (vs 1, go to Fig. 3)}$$

$$- T_K^{32} = -188.25 + 199.99 + 1 = 12.74$$

$$- T_b^{15} = 27.44 - 22.34 + 3.37 = 8.47 \text{ (vs 3.37)}$$

$$- T_b^{25} = 26.39 - 22.34 + 3.37 = 7.42$$

$$- T_b^{35} = 25.47 - 22.34 + 3.37 = 6.50$$

Socially desired outcomes

$$(C, H) > (B, \overline{H}) > (B, H) > (\overline{C}, H) > (C, \overline{H}) > (\overline{C}, \overline{H})$$

Sensitivity analyses

• If decrease Harden cost (K) below \$0.36 M, Harden becomes Utility's dominant strategy & (C, H) is Equilibrium (Fig. 4)

Why not (B, H)?

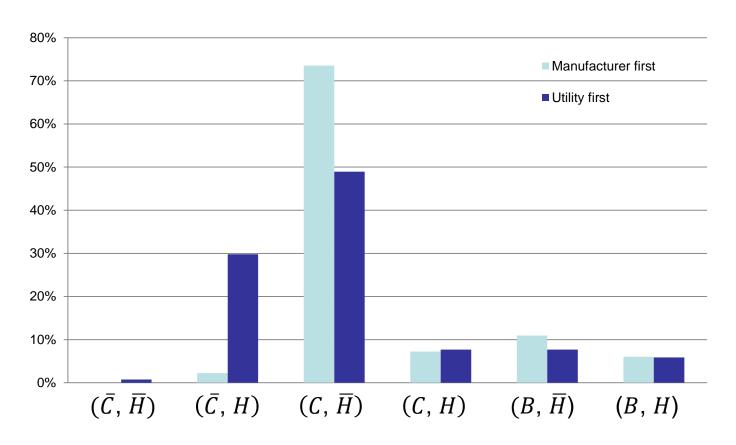
- $T_b^{46} = 24.67 24.69 + 3.37 = 3.35 (< 3.37)$
- Therefore, (C, H) is preferred to (B, H).
- However, if VOLL increases more than 15%, (B, H) is preferred since CHP + B/S provide more reliability improvement than Harden.
- What if outage duration is 12 hours instead of 24 hours?

Monte Carlo Simulation

- Above illustration is based on one set of parameters
- To account for uncertainty in the set of parameters, we use simulation to study ranges for certain parameters
- Simulation runs: 10,000
- Randomly varied parameters: CF of CHP: U(0%, 95%), Outage length l: U(0h, 48h), Prob. of outage given hardened grid p_H^l : U(0,0.2), Prob. of outage given unhardened grid p_N^l : U(0.7,0.9), Cost of grid hardening to utility and factory K:U(\$0, \$2M), c_H :U(\$0, \$0.2M), Electric consumption and hourly demand of the other user e^W (t):U(\$0, \$31.40M) & U(\$0, \$12,000), VOLL of the other user V^W : U(\$1.4, \$69,284)
- Varied decision variable: CHP incentive i∈{0, 5%, 10%, 15%, 20%, 25%, 30%} of CHP cost

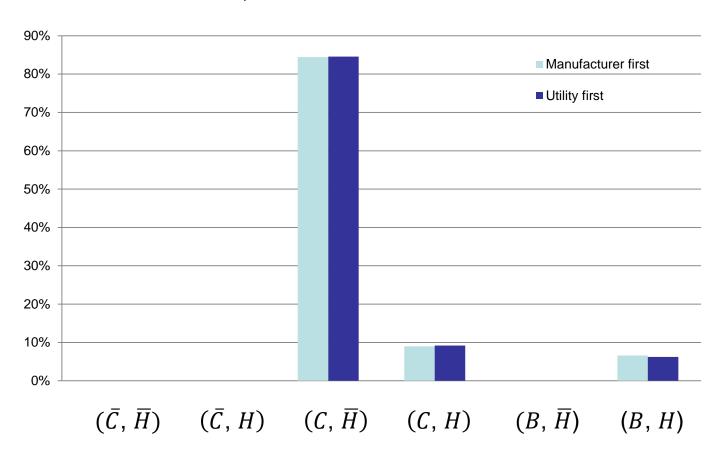
Simulation Result – Gas Turbine CHP

Order matters 53% of 10,000 runs



Simulation Result – Reciprocating Engine CHP

Order matters 17% of 10,000 runs



Conclusion

- Government might incentivize grid hardening & CHP (either with or without Blackstart capability but not both)
- If desired set of parameters are reached (perhaps after incentives), government could induce socially desirable outcomes
- In practice, with Gas Turbine (GT) CHP, socially desirable outcomes could be reached ((C, H)) or (B, \overline{H})
- Monte Carlo simulation shows
 - More outcomes could happen with GT CHP
 - With reciprocating engine CHP, only (C, H) can be reached
 - Regardless of CHP type, socially desirable outcomes could not be easily reached ((C, H) or (B, \overline{H})) suggesting investment in reducing the uncertainty of key parameters

Acknowledgement

This research is supported by the U.S. Department of Energy and the NJ Board of Public Utilities.

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Q&A?

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