### A Stochastic, Multi-Objective, Mixed-Integer Optimization Model for Biosolids Management program at the Blue Plains AWTP

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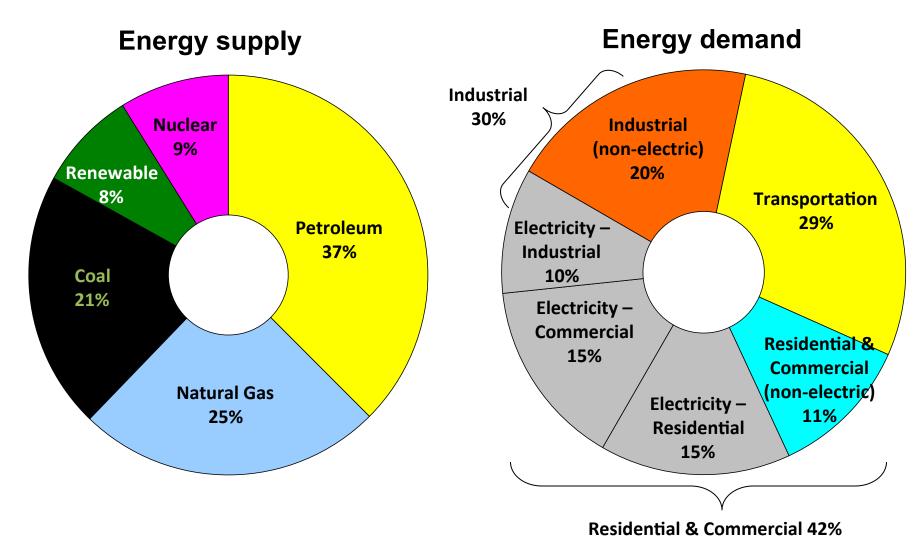




#### **Outline**

- Overview of energy and renewable energy
- The Blue Plains advanced wastewater treatment plant (AWTP) and biosolids management program
- Flowchart of modeling decisions/processes
- Preliminary results and discussion
- Conclusions
- Future work

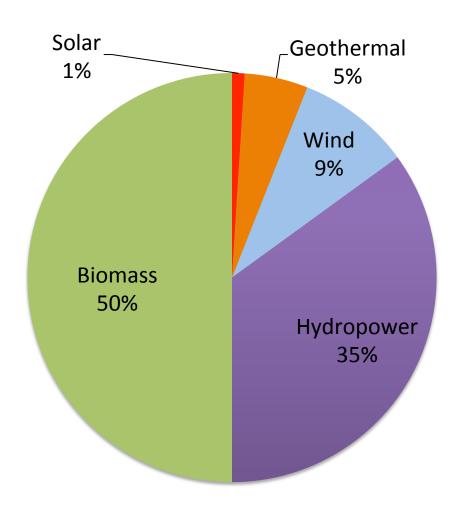
#### 2009 total U.S. energy use = 94.6 quadrillion BTU



Source: EIA Annual Energy Review 2009

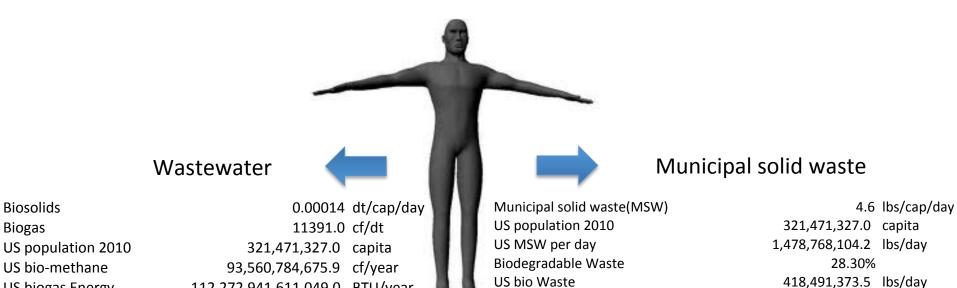
Richard Newell, December 16, 2010

#### 8% of the U.S. renewable energy use is about 7.6 quadrillion BTU



#### 1.7 quadrillion BTU can get from human's waste

### What's in Your Waste



112,272,941,611,049.0 BTU/year

Biosolids

**US** biogas Energy

Biogas

U.S. biogas as renewable energy potential is 1,425,774,944,697 cf/year or 1.7 quadrillion BTU/year (about 1.7% of US energy used in 2009)

US bio-methane

US biogas energy

1,332,214,160,021.1 cf/year

1,598,656,992,025,310.00 BTU/year

#### **Carbon Dioxide Emission Advantage from Waste**

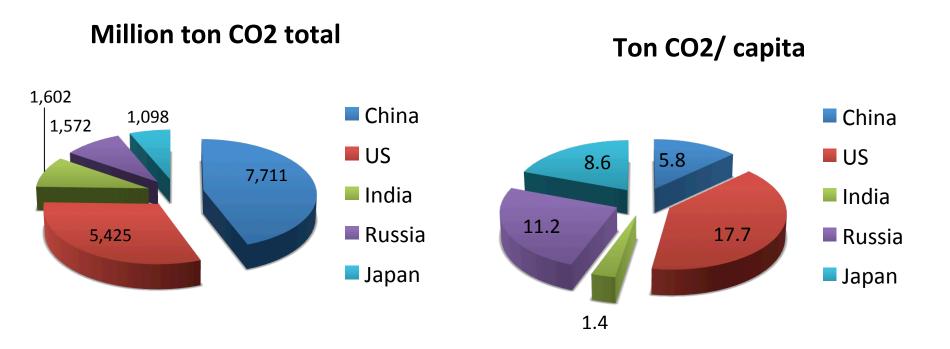
	Coal	Petroleum	Natural gas	Biomass		
				Wood	Landfill gas	WWT biogas
CO2 emission factor	103.62	73.15	53.06	93.87	52.07	52.07
kg CO2/MMBTU						
CO2 emission factor	-	-	0.0546	-	0.0262	≈0.0262
kg CO2/scf (for Gas)						

#### Note:

- 1. CO2 emission factors (per unit energy) are calculated as: Carbon Content × Fraction Oxidized × 44/12.
- 2. CO2 emission factors (per unit mass or volume) are calculated using: Heat Content  $\times$  Carbon Content  $\times$  Fraction Oxidized  $\times$  44/12  $\times$  Conversion Factor (if applicable). Heat content factors are based on higher heating values (HHV)
- 3. Waste from wastewater treatment plant produce WWT biogas
- 4. Municipal solid waste produce landfill gas

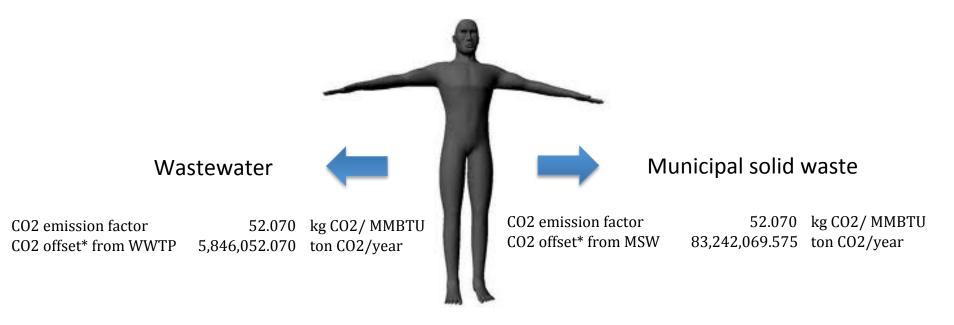
(Source: U.S. EPA Climate Leaders, Stationary Combustion Guidance (2007), Table B-2)

#### World Carbon Dioxide Emissions Data by Country



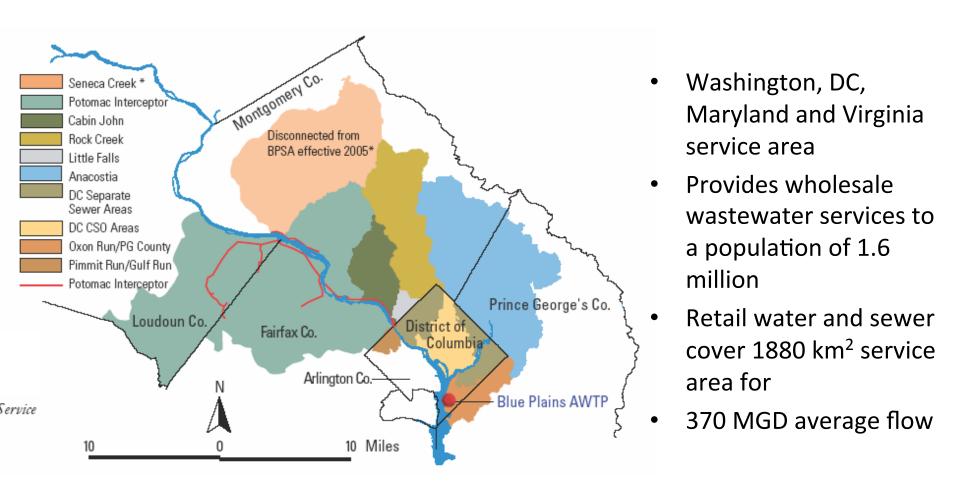
Source: http://www.guardian.co.uk/news/datablog/2011/jan/31/world-carbon-dioxide-emissions-country-data-co2 http://tonto.eia.doe.gov/cfapps/ipdbproject/IEDIndex3.cfm?tid=90&pid=44&aid=8

## CO<sub>2</sub> Offset from Using Your Waste

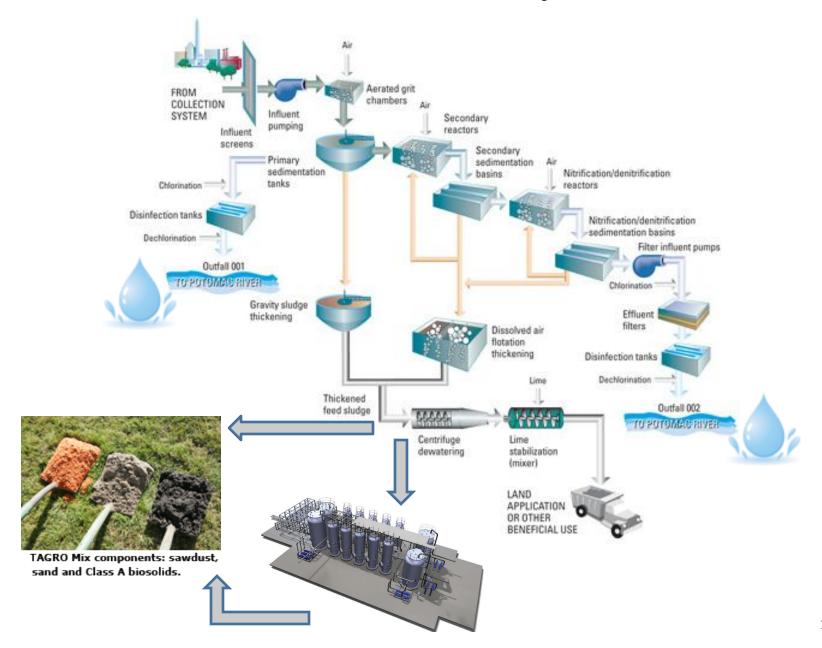


Use biogas from waste can offset 89,088,121.6 ton CO2/year (about 1.64 % of US CO<sub>2</sub> emission amount in 2009)

#### The Blue Plains AWTP, DC Water Service Area



#### The Blue Plains AWTP, DC Water Operational Process



Biosolids management program	Lime stabilization	Digester
Recover nutrients from the WWT process	Yes	Yes
Preserve farming in the Mid-Atlantic region	Yes	Yes
Quantity of biosolids	174-684dt/d	~180dt/d
Quality of biosolids	Class B	Class A + biogas
Generate carbon credits	How many?	How many?
Produce biogas for heat & power	NO	How much?
Cost of biosolids management	How much?	How much?
Benefit from byproduct (sold biosolids, sold biogas, sold electricity)	How much?	How much?

# This research uses a stochastic, multi-objective, optimization model under uncertainty to answer questions like "what we get from recycle biosolids"

 The first stage makes a decision "which process (digestion, producing Class A or Class B biosolids) will be the effective choice for Blue Plains to manage biosolids"







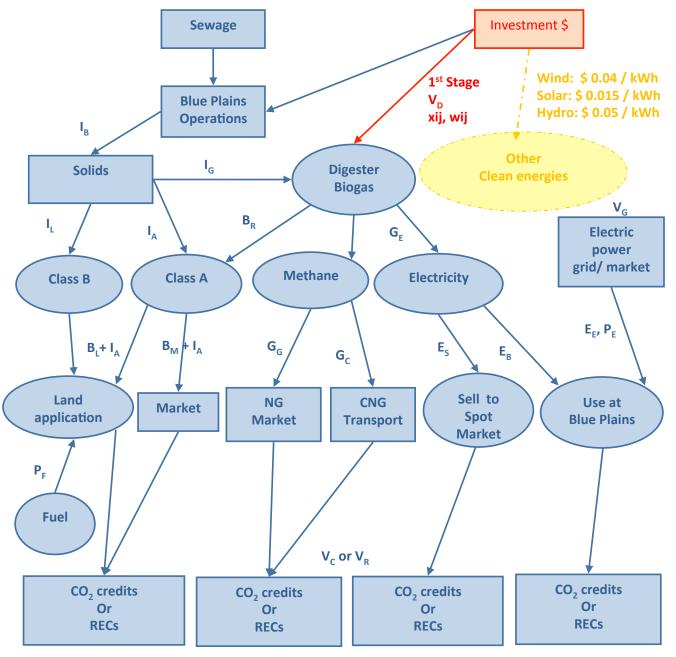
 The second stage answers questions, which are how many carbon credits we will get, how much energy we have to purchase, how much cost we can reduce







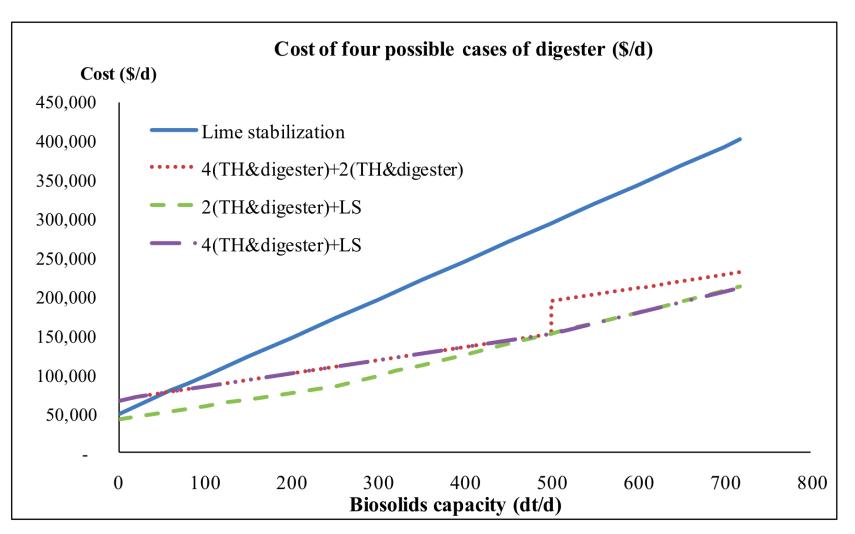




Flowchart for a stochastic multi-objective optimization model for biogas production at the Blue Plains AWTP, DC Water

#### 1<sup>st</sup> Stage Decision Variable

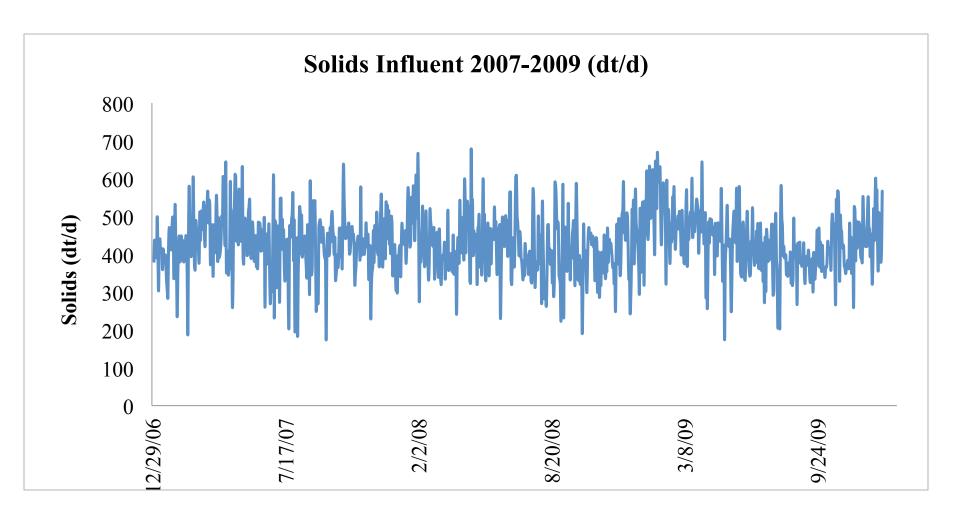
Four possible cases for construction and operational costs (50-years horizon) of digester related to biosolids capacity



#### **Uncertain Data Used in Stochastic Model**

- Solids influent data (inflow for digestion) in dry tons per day (dt/d)
- U.S. natural gas electric power prices in dollars per cubic feet (\$/cf)
- DC Water electricity consumption in kilo watt hour per day (kWh/d)
- U.S. electricity prices for PJM area in \$ per kilo watt hour (\$/kWh)
- DC water electricity cost in \$ per kilo watt hour (\$/kWh)
- Fossil fuel (Diesel) prices in \$ per gallon (\$/gallon)
- Biosolids as fertilizer prices in \$ per ton (\$/ton)
- Carbon credits in \$ per ton CO<sub>2</sub> equivalent (\$/ton CO<sub>2</sub> e)
- Renewable energy credits in \$ per ton CO<sub>2</sub> equivalent (\$/ton CO<sub>2</sub> e)
- Analyze probability distributions with ARENA software

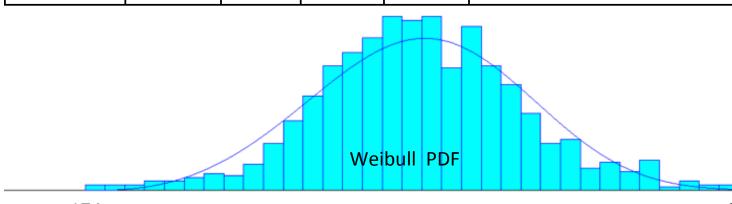
<sup>&</sup>quot;We will go over some examples of uncertainty data on the next slides"



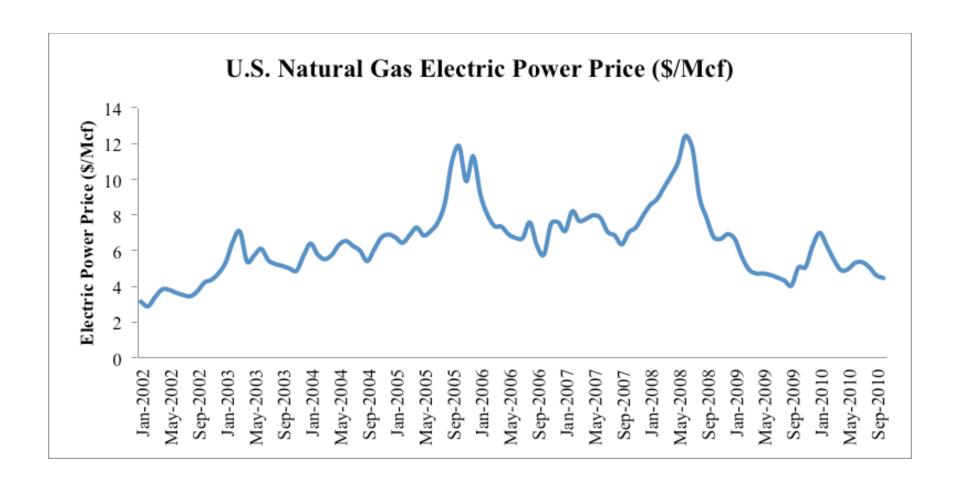
Solids influent for digester Solids influents are 174 - 684dt/d, data from 2007-2009 and project to 2030

#### **Probability Density Function of Solids Influent for Digester 2007-2009**

Distribution	Chi Squ	KS	Squ Err		Equation
Normal	<0.005	>0.15	0.00107	μ=429, σ=78.5	$f(x) = \begin{cases} \frac{1}{\sigma x \sqrt{2\pi}} e^{-(x-\mu)^2/(2\sigma)^2} & \text{for } x > 0\\ 0 & \text{otherwise} \end{cases}$
Beta	<0.005	0.0676	0.00153	$\beta$ =5.35, $\alpha$ =4.98	$f(x) = \begin{cases} \beta^{-\alpha} x^{\alpha - 1} e^{-x/\beta} & \text{for } 0 < x < 1\\ 0 & \text{otherwise} \end{cases}$
				α=4.98	( 0 otnerwise
Weibull*	< 0.005	0.106	0.00159	β=285,	$f(x) = \begin{cases} \alpha \beta^{-\alpha} x^{\alpha-1} e^{-(\frac{x}{\beta})^{\alpha}} & \text{for } x > 0\\ 0 & \text{otherwise} \end{cases}$
				α=3.59	
Erlang	< 0.005	< 0.01	0.00321	β=32,	$\left(\beta^{-k}x^{k-1}e^{-k/\beta}\right)$
				k=8	$f(x) = \begin{cases} \frac{\beta^{-k} x^{k-1} e^{-k/\beta}}{(k-1)!} & \text{for } x > 0\\ 0 & \text{otherwise} \end{cases}$



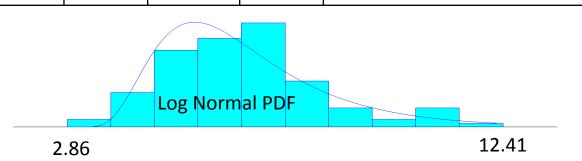
 $\frac{17}{684}$  dt/d<sup>17</sup>



U.S. Natural gas prices for electric power generation are 2.86-12.41 \$/ Mcf (2.76-11.97 \$/MMBtu), data from 2002-2010

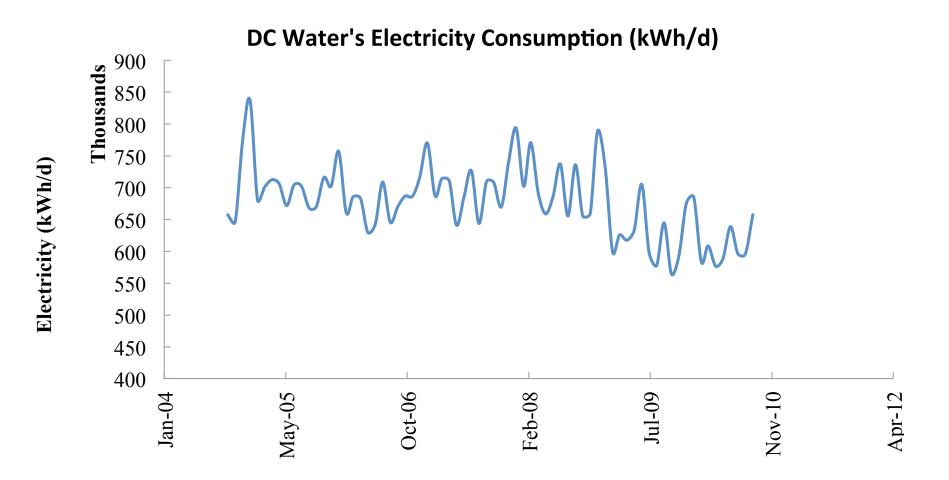
#### **Probability Density Function of U.S. Natural Gas Price 2002-2010**

Distribution	Chi Squ	KS	Squ Err		Equation
Erlang	0.21000	>0.15	0.00712	β=0.89, k=5	$f(x) = \begin{cases} \frac{\beta^{-k} x^{k-1} e^{-k/\beta}}{(k-1)!} & \text{for } x > 0\\ 0 & \text{otherwise} \end{cases}$
Gamma	0.21300	>0.15	0.00714	β=0.89, α=5.01	$f(x) = \begin{cases} \frac{\beta^{-\alpha} x^{\alpha - 1} e^{-x}/\beta}{\Gamma(\alpha)} & \text{for } x > 0 \\ 0 & \text{otherwise} \end{cases} \qquad \Gamma(\alpha) = \int_0^\infty t^{\alpha - 1} e^{-t} dt$
Weibull	0.09170	>0.15	0.00789	$\beta$ =5.04, $\alpha$ =2.41	$f(x) = \begin{cases} \alpha \beta^{-\alpha} x^{\alpha - 1} e^{-(\frac{x}{\beta})^{\alpha}} & \text{for } x > 0\\ 0 & \text{otherwise} \end{cases}$
Normal*	0.00876	>0.15	0.0115	μ=6.46, σ=1.96	$f(x) = \frac{1}{\sigma x \sqrt{2\pi}} e^{-(x-\mu)^2/(2\sigma)^2} \text{ for all real } x$
Beta	0.05390	>0.15	0.0108	β=2.64, α=3.88	$f(x) = \begin{cases} \frac{x^{\beta-1}(1-x)^{\alpha-1}}{B(\beta,\alpha)} & \text{for } 0 < x < 1\\ 0 & \text{otherwise} \end{cases}$ $B(\beta,\alpha) = \int_0^1 t^{\beta-1}(1-t)^{\alpha-1}dt$
Log normal*	0.07810	>0.15	0.0115	μ=4.51, σ=2.27	$f(x) = \begin{cases} \frac{1}{\sigma x \sqrt{2\pi}} e^{-(\ln(x) - \mu)^2/2\sigma^2} & \text{for } x > 0\\ 0 & \text{otherwise} \end{cases}$
Triangular	<0.0050	0.081	0.0232	a=260, m=304, b=360	$f(x) = \begin{cases} \frac{2(x-a)}{(m-a)(b-a)} & \text{for } a \le x \le m\\ \frac{2(b-x)}{(b-m)(b-a)} & \text{for } m \le x \le b \end{cases}$



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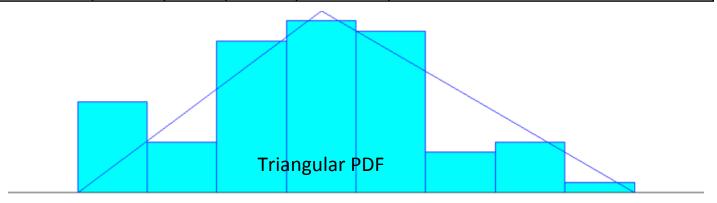
\$/Mcf



DC water electricity consumptions are about 564-838 MWh/d data from 2004-2010

#### Probability Density Function of DC Water Electricity Consumption 2000-2010

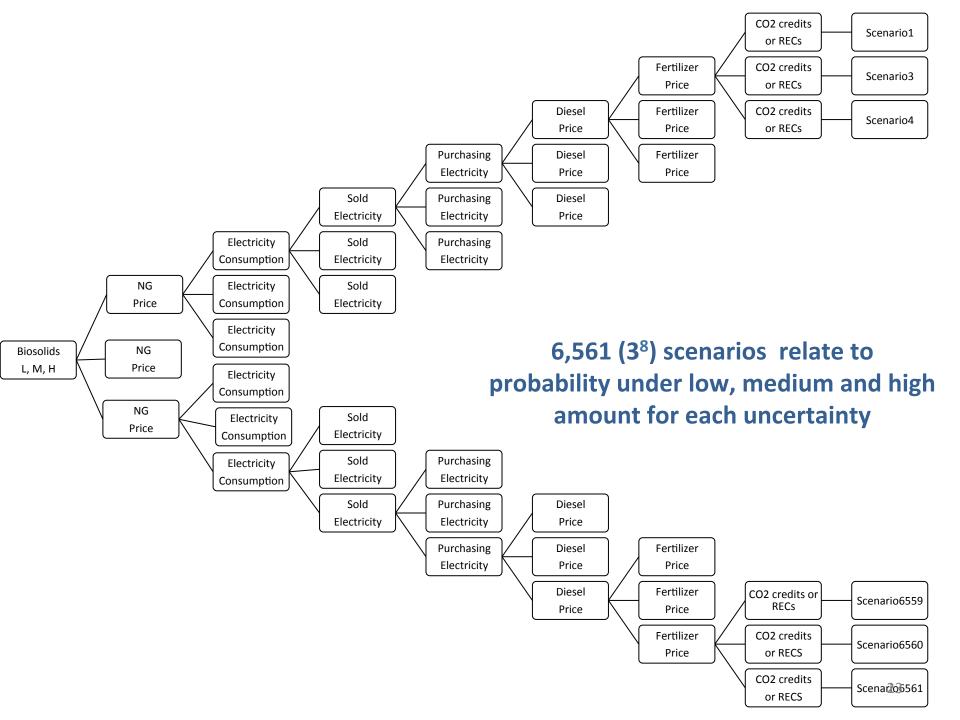
Distribution	Chi Squ	KS	Squ Err		Equation
Normal	0.722	>0.15	0.0130	μ=677000, σ=55600	$f(x) = \frac{1}{\sigma x \sqrt{2\pi}} e^{-(x-\mu)^2/2\sigma^2} \text{ for all real } x$
Triangular*	0.206	>0.018	0.0184	a=564000, m=684000, b=838000	$f(x) = \begin{cases} \frac{2(x-a)}{(m-a)(b-a)} & \text{for } a \le x \le m \\ \frac{2(b-x)}{(b-m)(b-a)} & \text{for } m \le x \le b \end{cases}$
Beta	0.078	>0.15	0.0209	β=1.95, α=2.78	$f(x) = \begin{cases} \frac{x^{\beta-1}(1-x)^{\alpha-1}}{B(\beta,\alpha)} & \text{for } 0 < x < 1\\ 0 & \text{otherwise} \end{cases}$ $B(\beta,\alpha) = \int_0^1 t^{\beta-1}(1-t)^{\alpha-1} dt$
Weibull	<0.005	0.034	0.0359	β=121000, α=1.57	$f(x) = \begin{cases} \alpha \beta^{-\alpha} x^{\alpha - 1} e^{-(\frac{x}{\beta})^{\alpha}} & \text{for } x > 0\\ 0 & \text{otherwise} \end{cases}$



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#### **Probability Density Function of all Uncertainty Data**

- 1. weibull biosolids influent PDF
- 2. log normal U.S. natural gas prices PDF
- 3. triangular DC Water electricity consumption PDF
- 4. log normal DC Water electricity cost PDF
- 5. log normal U.S. electric power prices PDF
- 6. triangular diesel prices PDF
- 7. weibull fertilizer prices PDF
- 8. triangular carbon credits PDF
- 9. Renewable energy credits \$1.89 per ton CO<sub>2</sub> e



#### A Stochastic Model for Biogas Production at the Blue Plains AWTP

#### Three objective functions

1. Minimize net carbon dioxide equivalent emission	(t/d)				
2. Minimize energy purchasing	(kWh/d)				
3. Maximize DC Water total value	(\$/d)				
s.t. 1 <sup>st</sup> stage constraints relate to digester investment cost	(\$/d)				
2 <sup>nd</sup> stage constraints relate to 6,561 scenarios					
- solids influent constraints	(dt/d)				
- biogas constraints	(cf/d)				
- biosolids class A constraints	(dt/d)				
<ul> <li>natural gas consumption constraints</li> </ul>	(cf/d)				
<ul> <li>electricity constraints with recourse</li> </ul>					
<ul> <li>carbon dioxide emission constraints</li> </ul>	(t/d)				
<ul> <li>energy consumption constraints</li> </ul>	(kWh/d)				
- value constraints (					

- Using Mixed-integer nonlinear programming (MINLP )and special ordered sets type 1 (SOS1) variables solve two-stage problem with recourse
- Optimization by General Algebraic Modeling System (GAMS)

#### **Preliminary Results and Discussion**

- Maximizing DC Water total value
- Here-and-Now (RP) result (two-stage stochastic model include risk and the capability to taking recourse problem)
- Expected results by using expected value (EVV), which fixed the 1<sup>st</sup> stage variable by using the bigger digester; four trains of thermal hydrolysis & anaerobic digester and using digester from RP result to find value of stochastic solution (VSS)
- Important of stochastic model for WWTP

# Here- and- Now (RP) for Maximizing DC Water Total Value Objective

- 1. First stage picked two trains of thermal hydrolysis & anaerobic digester up
- 2. Expected DC Water operational value \$-92,270 per day (cost)
- 3. Expected CO<sub>2</sub> e emissions is about 213.89 tons per day
- 4. Expected energy purchasing is about 425,070 kWh per day
- 5. Execution time for this model is about 12 hours

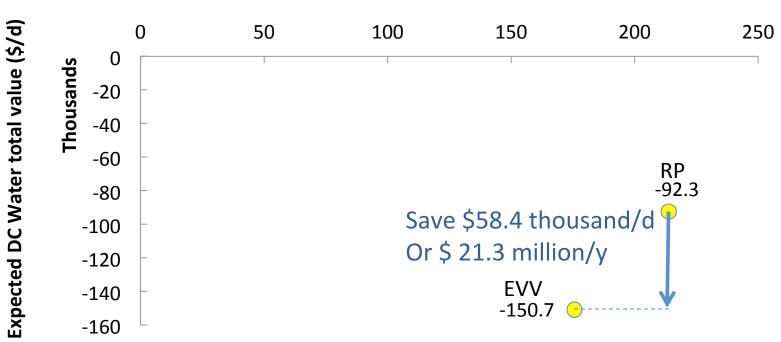
# How to Increase DC Water Total Value for Biosolids Management Program?

Cost (constraints in model)	Revenue (constraints in model)
Digester (construction and O&M)	Sold class A biosolids
Purchased electricity	Sold biogas
Delivering biosolids to the field	Sold electricity
	Carbon or renewable energy credits

Digester cost is the most influent variable for operational cost. Therefore DC Water should use the smallest digester in order to reduce digester cost, then generating electricity from biogas.

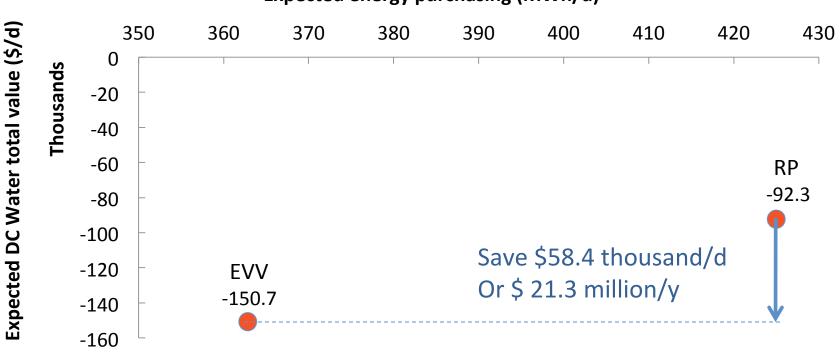
# Most Likely Solution (Fixed four trains of TH & anaerobic Digester) under Maximizing DC Water Total Value

Expected net carbon dioxide equivalent emission(ton/d)



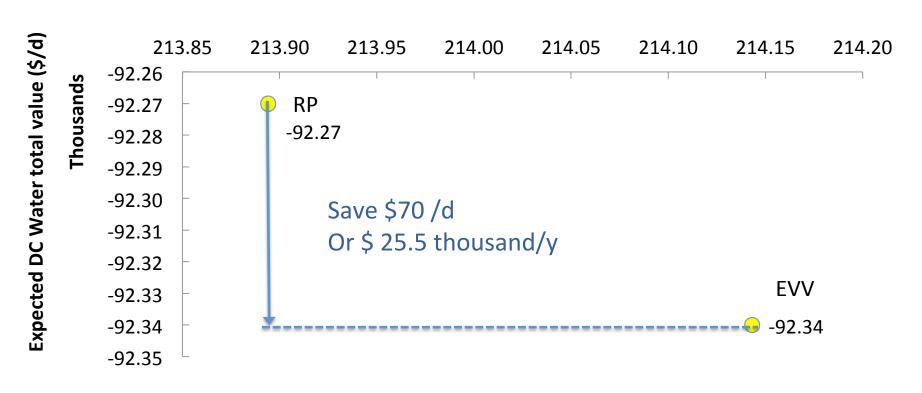
# Most Likely Solution (Fixed Four Trains of TH & anaerobic Digester) under Maximizing DC Water Total Value

#### Expected energy purchasing (MWh/d)



#### Value of stochastic solution under maximizing DC Water total value

#### Expected net carbon dioxide emission(ton/d)



#### **Conclusions**

- Stochastic model can help DC Water make a decision to use digester under real uncertain data and also reduce operation cost
- Results from maximizing DC Water total value may not be the best choice for DC Water if we have environmental concern
- This result supports multi-objective optimization idea (think both sides between economic and environment aspects).

#### **Future Work**

- Run stochastic model under other two objective functions, which are minimizing carbon dioxide equivalent emission and energy purchasing
- What is the best choice for DC Water considering under all three objective functions together? (Pareto optimal analysis)
- Add other investment choices of renewable energy sources

# Thank you